

第4章 2. 「対数」 第4回

解答

1. (1) 1 (2) 2 (3) -8 (4) -1 (5) 0 (6) $\frac{1}{4}$
2. (1) 6 (2) -1 (3) $2\log_2 3$ (4) 1 (5) -1 (6) 1
- (7) $\log_2 3$ (8) $\frac{5}{2}$
3. (1) $\frac{1}{2}$ (2) $\frac{1}{4}$
4. (1) $\frac{3}{2}$ (2) $\frac{3}{8}$

解説

1. (1) $\log_3 3 = m \iff 3^m = 3 = 3^1$ より $m = 1$
(2) $\log_{10} 100 = m \iff 10^m = 100 = 10^2$ より $m = 2$
(3) $\log_2 \frac{1}{256} = m \iff 2^m = \frac{1}{256} = 2^{-8}$ より $m = -8$
(4) $\log_2 0.5 = m \iff 2^m = 0.5 = \frac{1}{2} = 2^{-1}$ より $m = -1$
(5) $\log_{0.7} 1 = m \iff 0.7^m = 1 = 0.7^0$ より $m = 0$
(6) $\log_3 \sqrt[4]{3} = m \iff 3^m = \sqrt[4]{3} = 3^{\frac{1}{4}}$ より $m = \frac{1}{4}$
2. (1) 与式 $= \log_3 3^6 = 6\log_3 3 = 6 \times 1 = 6$
(2) 与式 $= \log_7 7^{-1} = -\log_7 7 = -1 \times 1 = -1$
(3) 与式 $= \log_2 (24 \times \frac{3}{8}) = \log_2 9 = \log_2 3^2 = 2\log_2 3$
(4) 与式 $= \log_5 (\frac{75}{8} \times \frac{8}{15}) = \log_5 5 = 1$
(5) 与式 $= \log_2 (42 \times \frac{1}{84}) = \log_2 \frac{1}{2} = \log_2 2^{-1} = -1 \times \log_2 2 = -1 \times 1 = -1$
(6) 与式 $= \log_3 (\frac{28}{3} \times \frac{9}{28}) = \log_3 3 = 1$
(7) 与式 $= \log_2 3^{\frac{2}{3}} + \log_2 3^{\frac{1}{3}} = \log_2 3^{\frac{2}{3} + \frac{1}{3}} = \log_2 3^1 = \log_2 3$
(8) 与式 $= \log_2 (\sqrt{10} \times \frac{4}{\sqrt{5}}) = \log_2 4\sqrt{2} = \log_2 (2^2 \times 2^{\frac{1}{2}}) = \log_2 2^{2+\frac{1}{2}} = \log_2 2^{\frac{5}{2}} = \frac{5}{2} \log_2 2 = \frac{5}{2}$
3. (1) 与式 $= \frac{1}{\log_2 4} = \frac{1}{\log_2 2^2} = \frac{1}{2\log_2 2} = \frac{1}{2}$
(2) 与式 $= \frac{1}{\log_3 81} = \frac{1}{\log_3 3^4} = \frac{1}{4\log_3 3} = \frac{1}{4}$
4. (1) 底を2に変換して、与式 $= \frac{\log_2 27}{\log_2 4} \times \frac{\log_2 2}{\log_2 3} = \frac{\log_2 3^3}{\log_2 2^2} \times \frac{1}{\log_2 3} = \frac{3\log_2 3}{2\log_2 2} \times \frac{1}{\log_2 3} = \frac{3}{2}$
(2) 底を2に変換して、与式 $= \frac{\log_2 9}{\log_2 16} \times \frac{\log_2 8}{\log_2 81} = \frac{\log_2 3^2}{\log_2 2^4} \times \frac{\log_2 2^3}{\log_2 3^4} = \frac{2\log_2 3}{4\log_2 2} \times \frac{3\log_2 2}{4\log_2 3} = \frac{2\log_2 3}{4} \times \frac{3}{4\log_2 3} = \frac{3}{8}$